

MAFS.912.F-BF.2.3	Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$, $kf(x)$, $f(kx)$, and $f(x + k)$ for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. <i>Include recognizing even and odd functions from their graphs and algebraic expressions for them.</i>
Item Types	<p>Equation Editor – May require creating a value or an expression.</p> <p>GRID – May require plotting points or a transformed function.</p> <p>Matching Item – May require matching an equation, a value of k, and an explanation of the effect on a graph.</p> <p>Multiple Choice – May require selecting a graph or a table from a list.</p> <p>Open Response – May require explaining the effects of a transformation.</p> <p>Table Item – May require completing a table of values.</p>
Clarifications	<p>Students will determine the value of k when given a graph of the function and its transformation.</p> <p>Students will identify differences and similarities between a function and its transformation.</p> <p>Students will identify a graph of a function given a graph or a table of a transformation and the type of transformation that is represented.</p> <p>Students will graph by applying a given transformation to a function.</p> <p>Students will identify ordered pairs of a transformed graph.</p> <p>Students will complete a table for a transformed function.</p>
Assessment Limits	<p>Functions represented algebraically are limited to linear, quadratic, or exponential.</p> <p>Functions represented using tables or graphs are not limited to linear, quadratic, or exponential.</p> <p>Functions may be represented using tables or graphs.</p> <p>Functions may have closed domains.</p> <p>Functions may be discontinuous.</p> <p>Items should have a single transformation.</p>
Stimulus Attributes	<p>Items should be given in a mathematical context.</p> <p>Items may use function notation.</p>

	Items may present a function using an equation, a table of values, or a graph.
Response Attributes	<p>Items may require the student to explain or justify a transformation that has been applied to a function.</p> <p>Items may require the student to explain how a graph is affected by a value of k.</p> <p>Items may require the student to find the value of k.</p> <p>Items may require the student to complete a table of values.</p>
Calculator	Neutral

Sample Item	Item Type																								
<p>The table below shows the values for the function $y = f(x)$.</p> <table border="1" style="display: inline-table; margin-right: 20px;"> <thead> <tr> <th>x</th> <th>y</th> </tr> </thead> <tbody> <tr><td><input type="text"/></td><td><input type="text"/></td></tr> </tbody> </table> <table border="1" style="display: inline-table;"> <thead> <tr> <th>x</th> <th>y</th> </tr> </thead> <tbody> <tr><td>-4</td><td>7</td></tr> <tr><td>-1</td><td>-2</td></tr> <tr><td>0</td><td>3</td></tr> <tr><td>3</td><td>-4</td></tr> <tr><td>6</td><td>5</td></tr> </tbody> </table> <p>Complete the table for the function $y = f\left(\frac{1}{5}x\right)$.</p>	x	y	<input type="text"/>	x	y	-4	7	-1	-2	0	3	3	-4	6	5	Table Item									
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